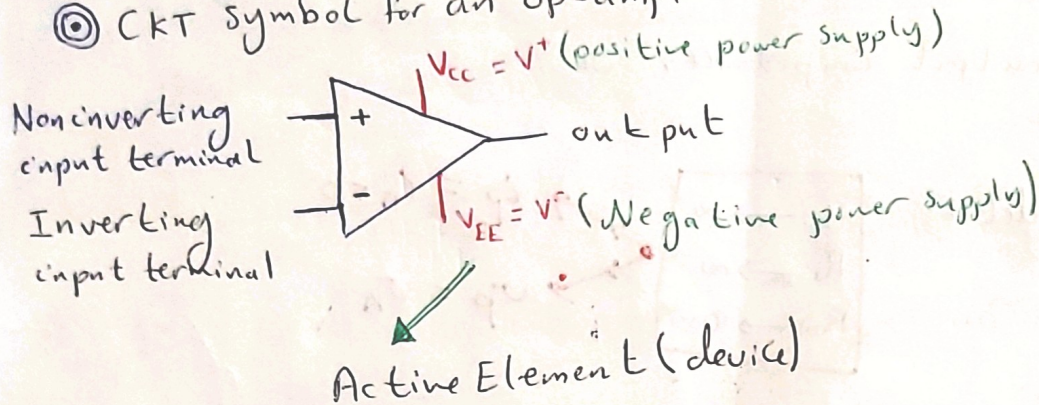


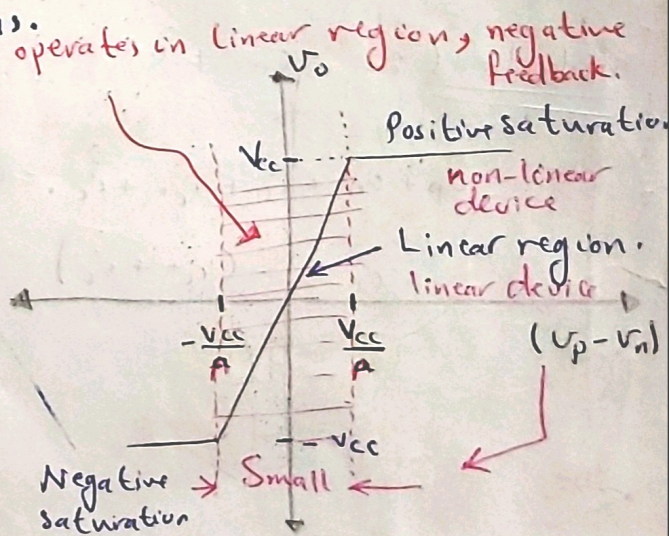
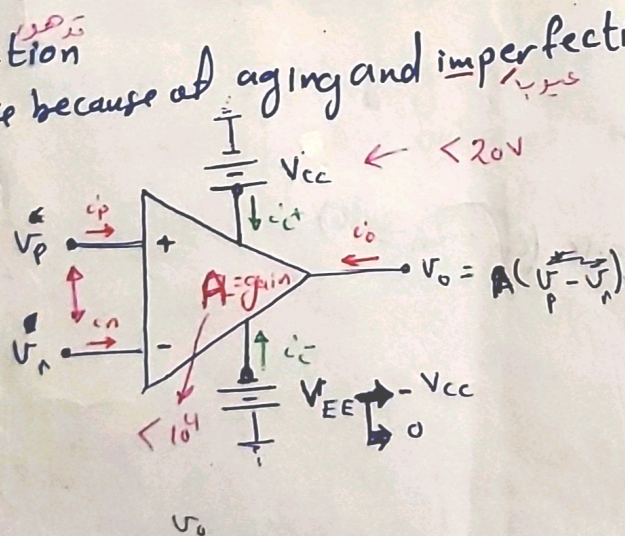
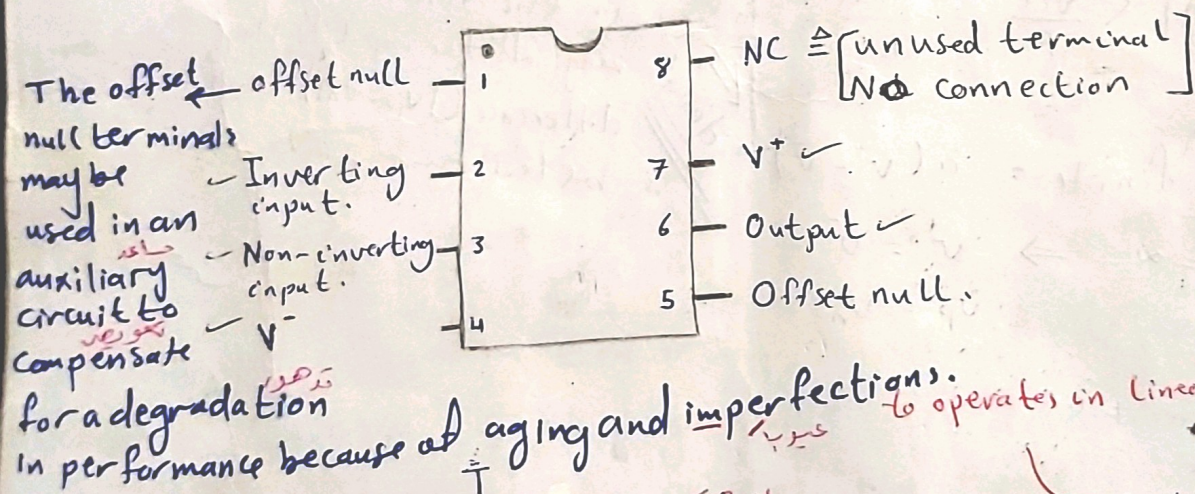
The Operational Amplifier ((Op-amp))

* It was referred to as operational because it was used to implement the mathematical operations of integration, differentiation, addition, sign changing, and scaling.

◎ CKT symbol for an op-amp.

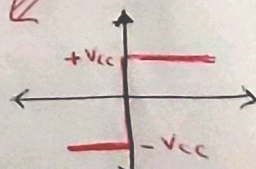


◎ commercially available device (741)



$$V_o = \begin{cases} +V_{cc} & A(V_p - V_n) > +V_{cc} \\ -V_{cc} & A(V_p - V_n) < -V_{cc} \\ A(V_p - V_n) & -V_{cc} \leq A(V_p - V_n) \leq +V_{cc} \end{cases}$$

• The voltage transfer characteristic of an op amp.

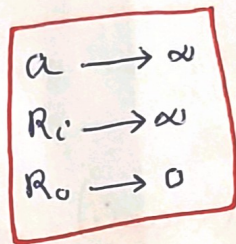


$$i_p + i_n + i_o + i_{c+} + i_{c-} = 0$$

OP-Amp Properties :-

- 1) Very large gain [Ratio between v_o, v_i], a
10,000
- 2) Very large input impedance. $M\Omega$
- 3) Very small output impedance. Ω

Ideal Op-amp Model :-



$i_p = i_n = 0$

$v_p = v_n$

1) $i_p = i_n = 0$

2) $|v_o| < +V_{cc}$

$|A(v_p - v_n)| < V_{cc}$

$|v_p - v_n| < \frac{V_{cc}}{A} = \frac{20V}{10^4} \approx 2mV$

in the linear region, the mag. of the input voltage difference ($|v_p - v_n|$) must be less than 2mV

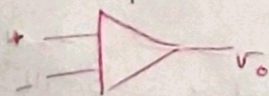
2) $v_o = v_{finite} = a(v^+ - v^-)$

$\frac{v_o}{a} = (v^+ - v^-), a \approx \infty \Rightarrow v^+ = v^-$
 $v_p = v_n$

note that : $i_o \neq 0$

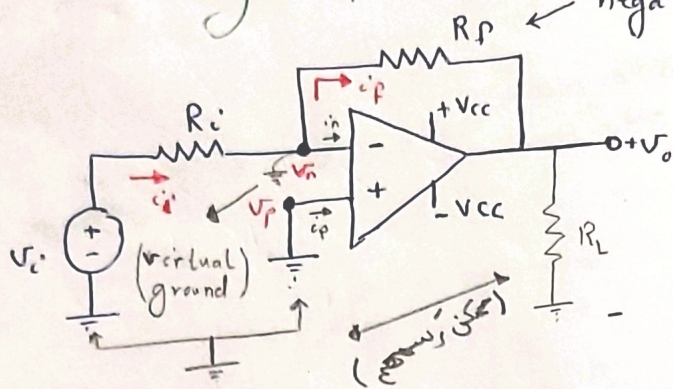
$i_p + i_n + i_o + i_c^+ + i_c^- = 0$

$i_o = -(i_c^+ + i_c^-)$ since $(i_p = i_n = 0)$



Some Important Op-Amp Circuits

□ Inverting Amplifier :- negative feedback.



$$V_p = V_n$$

$$i_p = i_n = 0$$

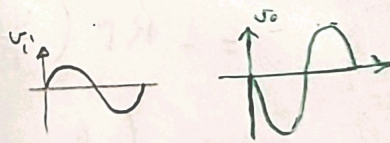
□ Since $V_p = 0$, $V_n = V_p = 0$

$$i_i = \frac{V_i}{R_i}$$

□ Since $i_n = i_p = 0 \Rightarrow i_f = i_i = \frac{V_i}{R_i}$

$$\therefore V_o = -R_f i_f = -R_f \left[\frac{V_i}{R_i} \right] = -\frac{R_f}{R_i} V_i$$

$$\frac{V_o}{V_i} = \text{gain} = -\frac{R_f}{R_i}$$



→ inverting, input from inv terminal

* The upper limit on the gain $\frac{R_f}{R_i}$, is determined by the power supply voltages and the value of R_i the signal voltage V_i .

→ if $V^+ = V^- \Rightarrow V_{cc} = V_{EE} = V_{cc}$

$$|V_o| \leq V_{cc}$$

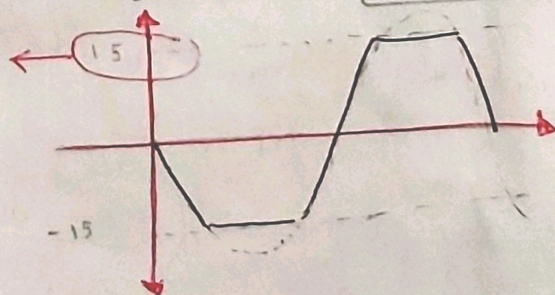
$$\left| \frac{R_f}{R_i} V_i \right| \leq V_{cc}$$

$$\frac{R_f}{R_i} \leq \left| \frac{V_{cc}}{V_i} \right|$$

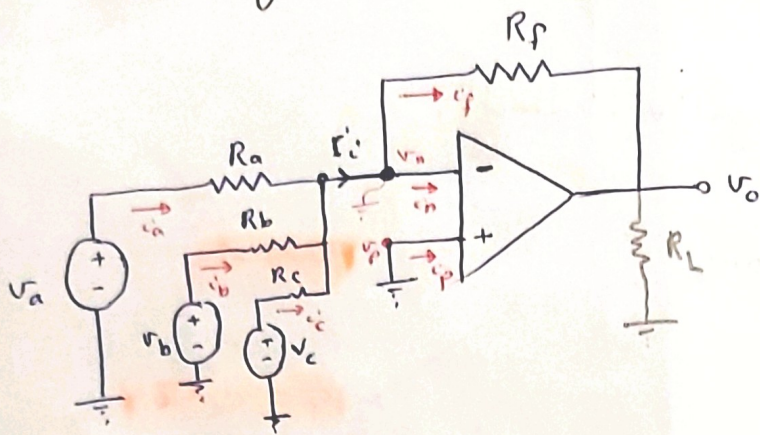
if $V_{cc} = 15V$
 $V_i = 10mV$

$$\frac{R_f}{R_i} \leq 1500$$

practically not 15-E



7] Inverting Adder ((Summing Amplifier)) ((Mixer))
 (مختلج)
 (مختلط)



a) Since $v_p = 0 \Rightarrow v_p = v_n = 0$

$$i_a = \frac{v_a}{R_a}, \quad i_b = \frac{v_b}{R_b}, \quad i_c = \frac{v_c}{R_c}$$

$$i_i = i_a + i_b + i_c$$

b) Since $i_n = i_p = 0 \Rightarrow i_i = i_f$

$$v_o = -R_f i_f = -R_f (i_a + i_b + i_c)$$

$$= -R_f \left(\frac{v_a}{R_a} + \frac{v_b}{R_b} + \frac{v_c}{R_c} \right)$$

$$= - \left(\frac{R_f}{R_a} v_a + \frac{R_f}{R_b} v_b + \frac{R_f}{R_c} v_c \right)$$

Special Cases

i) if $R_a = R_b = R_c = R_i$

$$v_o = - \frac{R_f}{R_i} (v_a + v_b + v_c)$$

ii) if $R_a = R_b = R_c = R_i = R_f$

$$v_o = -(v_a + v_b + v_c) \quad \text{op-amp as an adder}$$

iii) if $R_a = R_b = R_c = R_i$, and

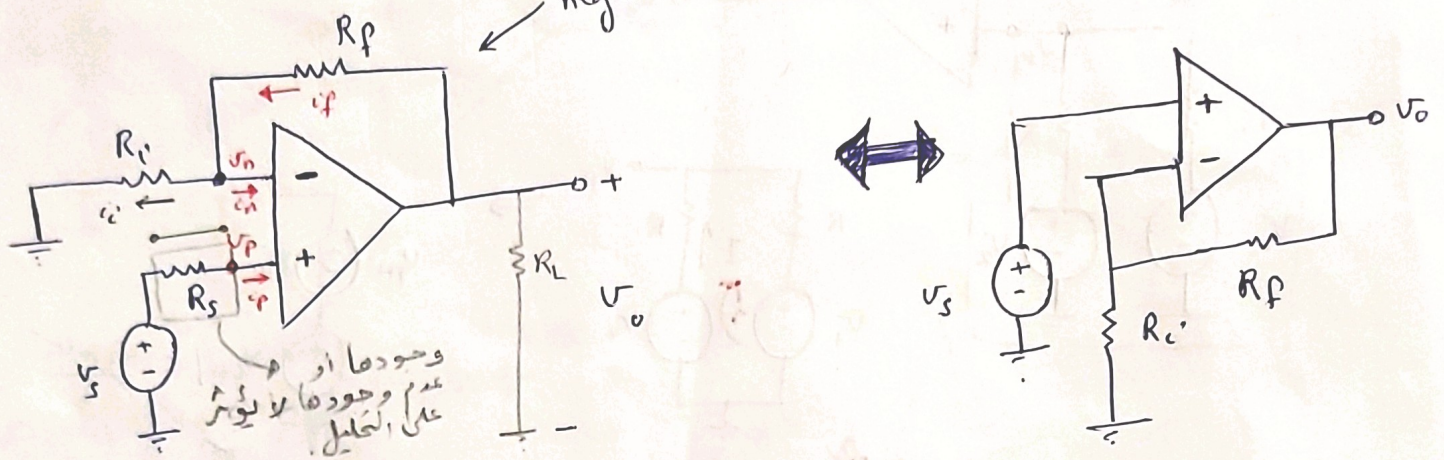
$$R_f = \frac{R_i}{3}$$

$$v_o = - \left(\frac{v_a + v_b + v_c}{3} \right) \quad \text{((average))}$$

3) Non-inverting Amplifier:-

- non-inverting input terminal
- output = (gain) (v_i)

negative feedback.



* Since $v_p = v_n \Rightarrow v_p = v_s$ because $(v_n = v_p = 0)$

$$v_i = \frac{v_s - 0}{R_i} = \frac{v_s}{R_i}$$

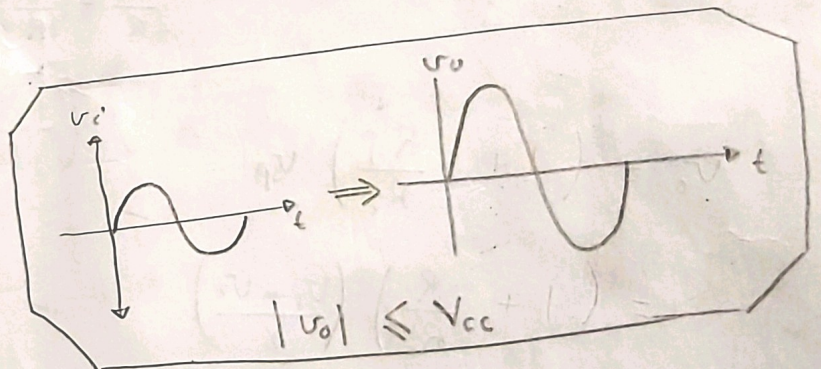
* Since $v_n = 0 \Rightarrow v_i = v_p$

$$v_o = R_f v_i + v_s$$

$$= R_f \left(\frac{v_s}{R_i} \right) + v_s$$

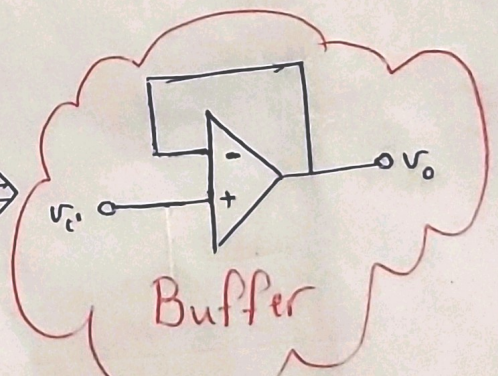
$$v_o = \left(1 + \frac{R_f}{R_i} \right) v_s$$

$$\boxed{\frac{v_o}{v_i} = \text{gain} = 1 + \frac{R_f}{R_i}}$$



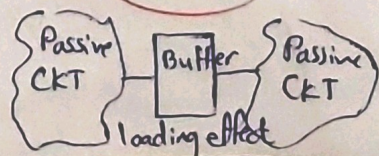
Special Case:-

- if $R_i = \infty$ (open CKT) \Rightarrow $v_i = v_o$ (مساوية)
- $R_f = 0$ (short CKT) \Rightarrow $v_i = v_o$ (سلك)

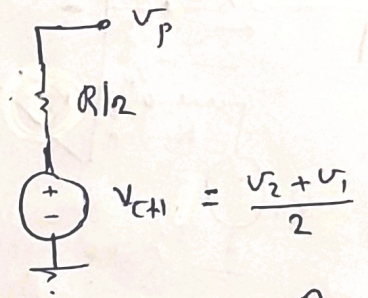
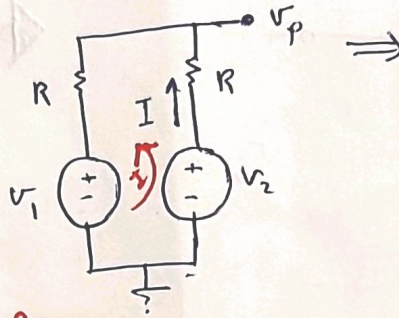
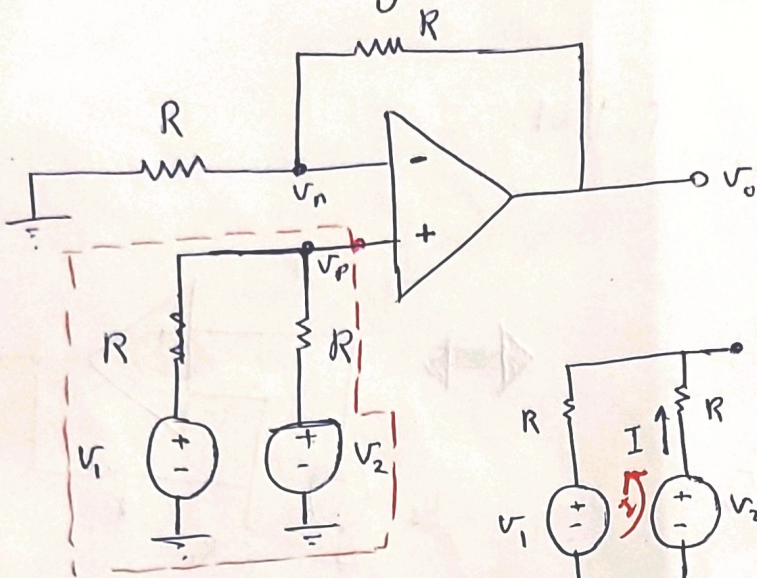


$$\frac{v_o}{v_i} = 1 = A \triangleq \text{unity gain Amplifier}$$

$$\triangleq \text{Buffer}$$



4) Non-inverting Adder (Summing Amp) (Mixer)



Loop

$$V_2 = RI + RI + V_1 =$$

$$I = \frac{V_2 - V_1}{2R}$$

$$= \frac{V_2}{2R} - \frac{V_1}{2R}$$

$$R_{TH} = R_{OC} = \frac{R}{2}$$

$$V_{TH} = -RI + V_2$$

$$= -\frac{V_2}{2} + \frac{V_1}{2} + V_2$$

$$= \frac{V_2}{2} + \frac{V_1}{2}$$

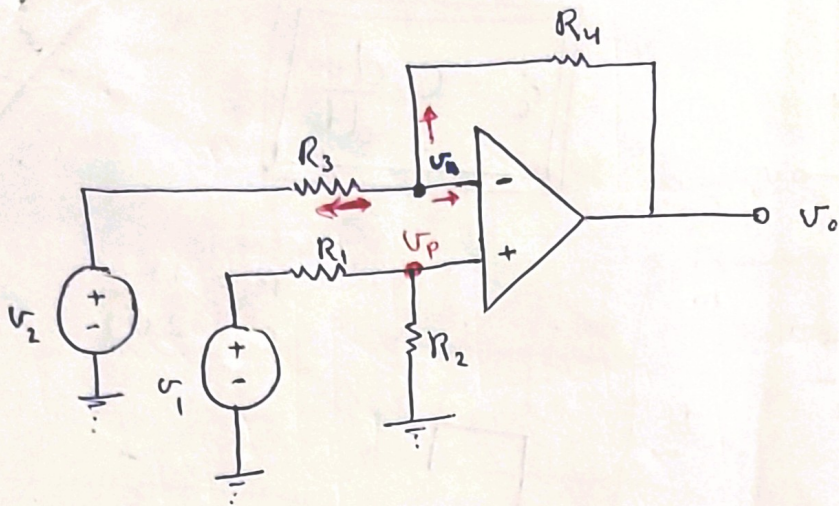
$$= \frac{V_2 + V_1}{2}$$

$$V_0 = \left(1 + \frac{R_f}{R_i}\right) V_i$$

$$= \left(1 + \frac{R}{R}\right) \left(\frac{V_1 + V_2}{2}\right)$$

$$V_0 = V_1 + V_2$$

5) Difference Amplifier ((Voltage Subtraction))



$$\frac{v_n - v_2}{R_3} + \frac{v_n - v_0}{R_4} + i_n = 0$$

* $i_n = 0$

* $v_p = v_n = \frac{R_2}{R_2 + R_1} v_1$

Using superposition :-

$$v_0 = \overset{\text{kill } v_1}{v_{01}} + \overset{\text{kill } v_2}{v_{02}}$$

$$= v_2 \left(-\frac{R_4}{R_3} \right) + \left(1 + \frac{R_4}{R_3} \right) v_p \quad \leftarrow \text{voltage divider}$$

$$= v_2 \left(-\frac{R_4}{R_3} \right) + \left(1 + \frac{R_4}{R_3} \right) \left(\frac{R_2}{R_1 + R_2} \right) v_1$$

$\underbrace{\hspace{10em}}_b \quad \underbrace{\hspace{10em}}_a$

$$= a v_1 - b v_2$$

if $R_4 = \infty$
 $R_3 = 0$
 $R_2 = \infty$
 $R_1 = 0$

$$v_0 = v_2 (-\infty) + (1 + \infty)(\infty)v_1$$

Special Case :-

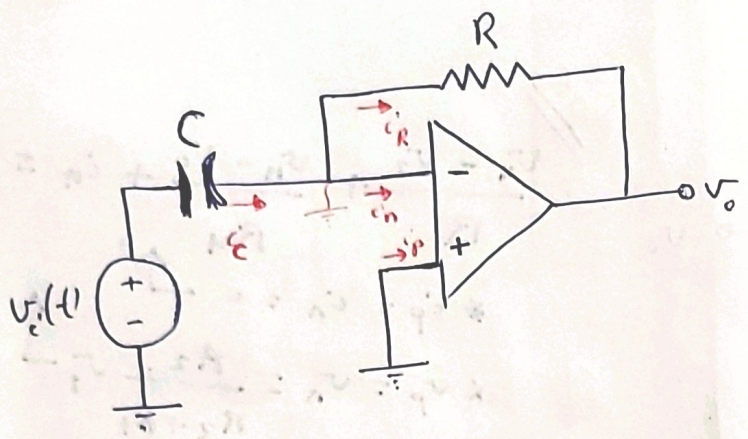
$$\frac{R_2}{R_1} = \frac{R_4}{R_3} = A \Rightarrow A = \left(\frac{R_2}{R_1} \right) = \left(\frac{R_4}{R_3} \right)$$

$$v_0 = A (v_1 - v_2)$$

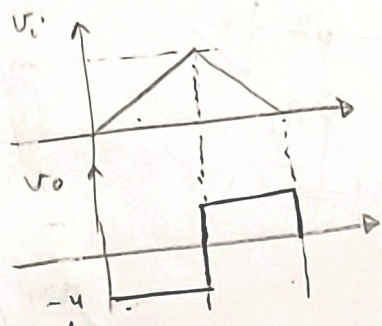
$$= -v_2 \left(\frac{aR}{A} \right) + \left(1 + \frac{aR}{A} \right) \left(\frac{aR}{A + aR} \right) v_1$$

$$= -av_2 + (1 + a) \left(\frac{a}{1 + a} \right) v_1$$

6) Differentiator



$$i_c = C \frac{dv}{dt}$$



$$i_c = i_R$$

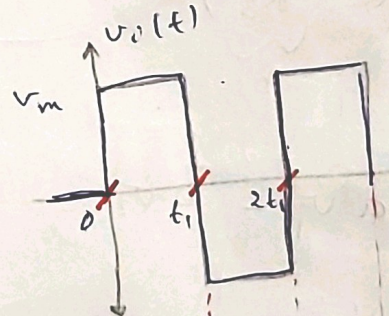
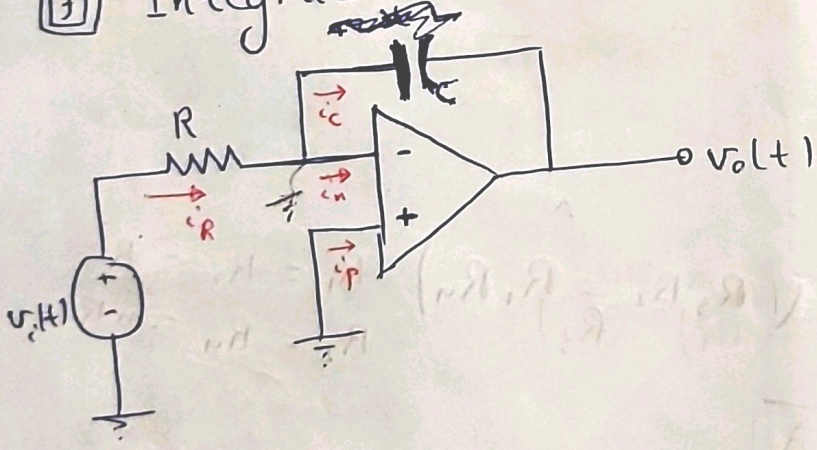
$$C \frac{dv_c}{dt} = i_R = C \frac{d}{dt} (v_i(t) - 0) = C \frac{dv_i}{dt}$$

$$v_o = -R i_R = -R \left[C \frac{dv_i}{dt} \right] = -RC \frac{dv_i(t)}{dt}$$

$$v_o(t) = -RC \frac{dv_i(t)}{dt}$$

* $i_c(t) = C \frac{dv}{dt}$
 $v(t) = \frac{1}{C} \int i_c dt + v(t_0)$
 in many practical app. the initial time is zero, $t_0 = 0$
 $v(t) = \frac{1}{C} \int_0^t i_c dt + v(t_0)$

7) Integrator



assume that the initial value of $v_o(t)$ is zero at the instant v_i steps from 0 to v_m

$$v_o = -\frac{1}{RC} v_m t + v_o$$

$$0 \leq t \leq t_1$$

$$v_o = -\frac{1}{RC} \int_{t_1}^t v_m dt - \frac{1}{RC} v_m t_1$$

$$= \frac{v_m}{RC} t - \frac{2v_m t_1}{RC}$$

$$t_1 \leq t \leq 2t_1$$

$$i_R = \frac{v_i(t)}{R}$$

$$v_o(t) = -v_c(t) = -\frac{1}{C} \int_{t_0}^t i_c dt + v_o(t_0)$$

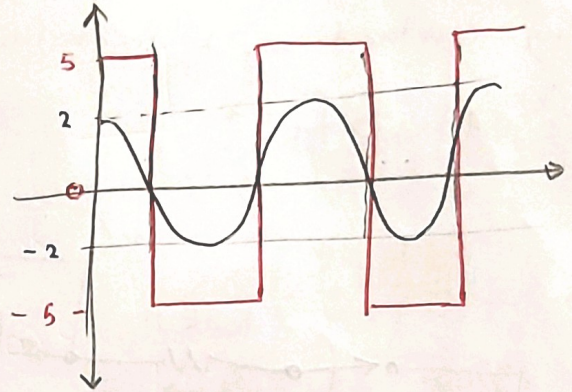
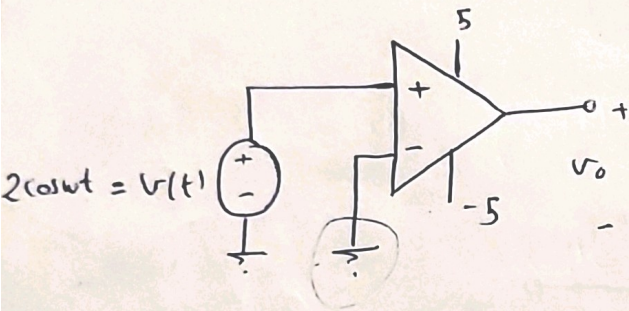
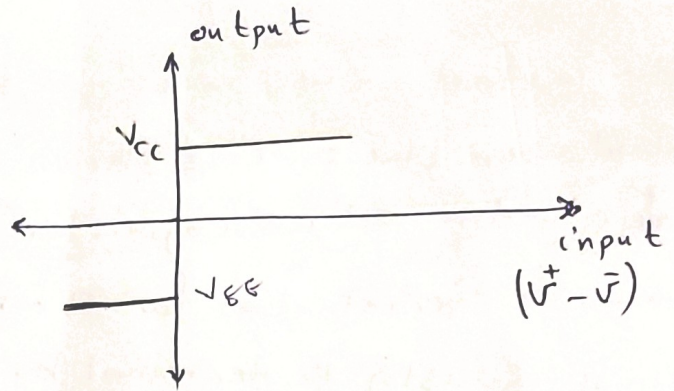
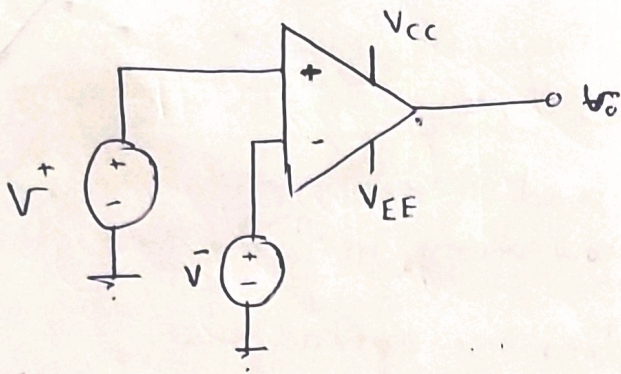
$$v_o(t) = -\frac{1}{RC} \int_{t_0}^t v_i(t) dt + v_o(t_0)$$

if $t_0 = 0$

Capacitor initially discharged

$$= -\frac{1}{RC} \int_0^t v_i(t) dt + v_o(0)$$

8) Comparators



9) Other Op-Amp CKTs

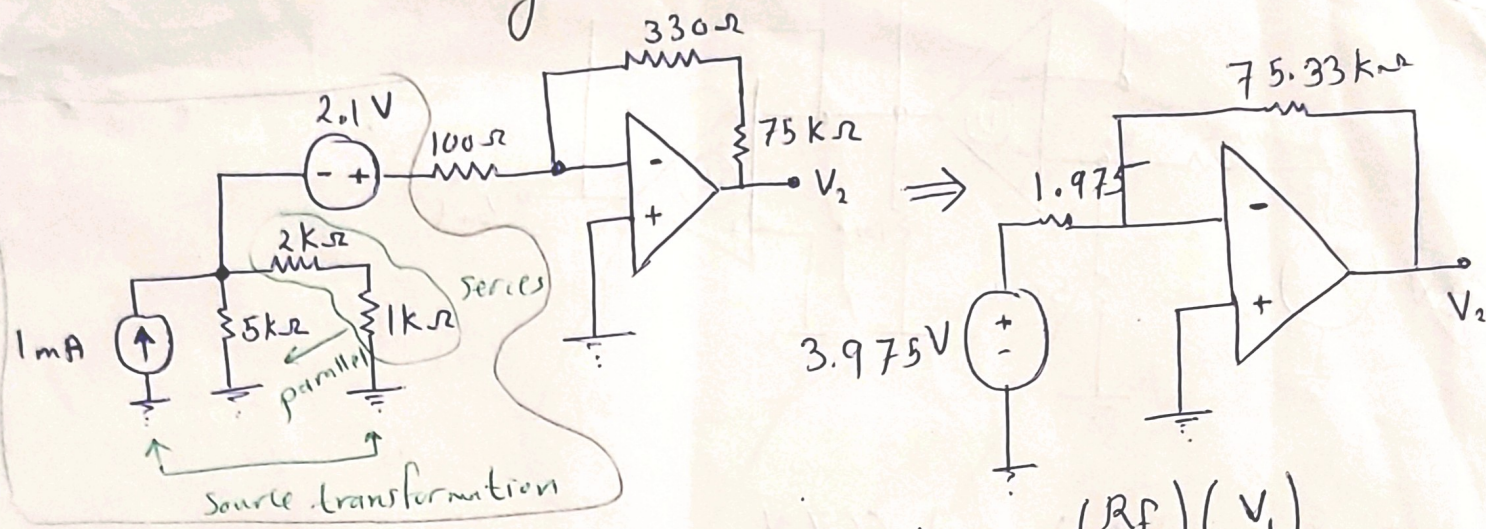
Use:-
 (a) $i_p = i_n = 0$, $v_p = v_n$

(b) Apply nodal analysis to the resulting CKT

(c) Solve nodal equations to express the output voltage in terms of the op-amp input signals.

Examples

1) For the circuit of Figure E1, Calculate the voltage V_2 .

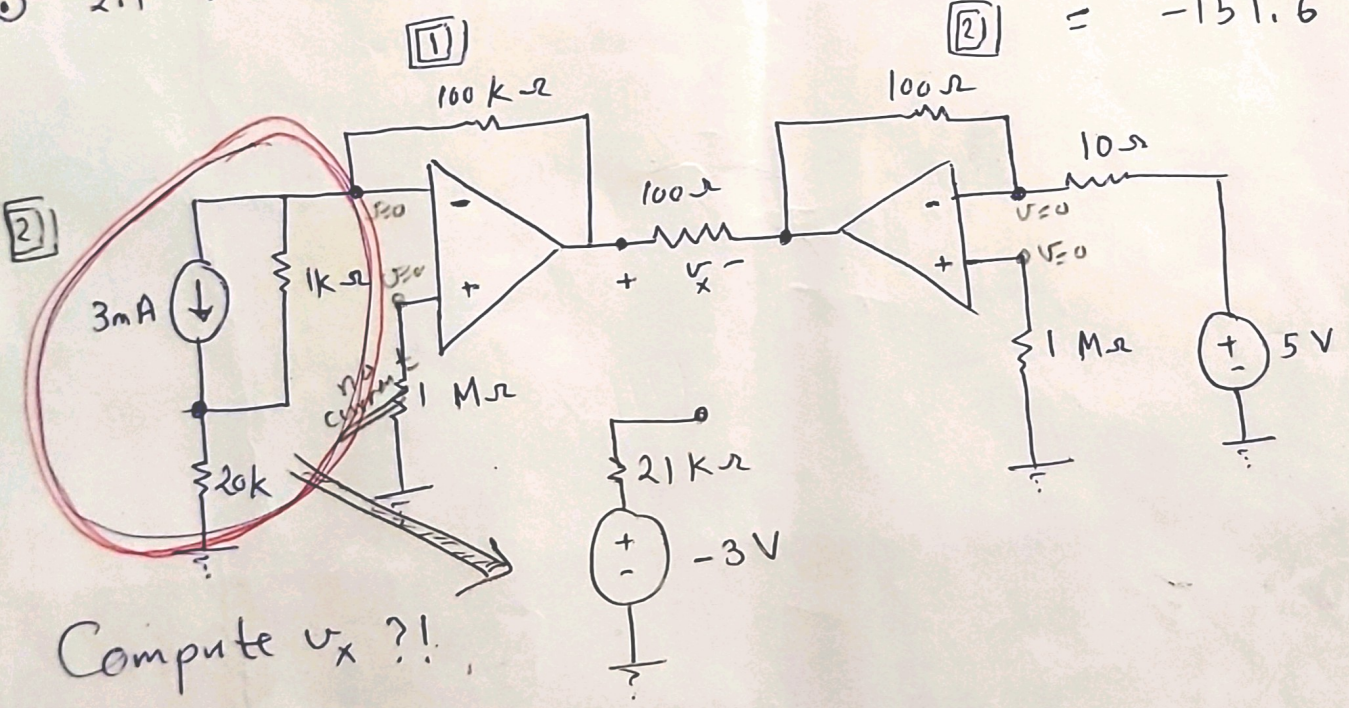


- 1) $(5k \parallel 1k) = 1.875k\Omega$
- 2) $(1mA)(1.875k\Omega) = 1.875V$
- 3) $2.1V + 1.875V = 3.975V$

$$V_2 = -\left(\frac{R_F}{R_i}\right)(V_1)$$

$$= -\left(\frac{75.33k}{1.975k}\right)(3.975)$$

$$= -151.6V$$



Compute V_x ?!

$$V_{out1} = -\left(\frac{100k}{21k}\right)(-3) = 14.29$$

$$V_{out2} = -\left(\frac{100}{10}\right)(5) = -50$$

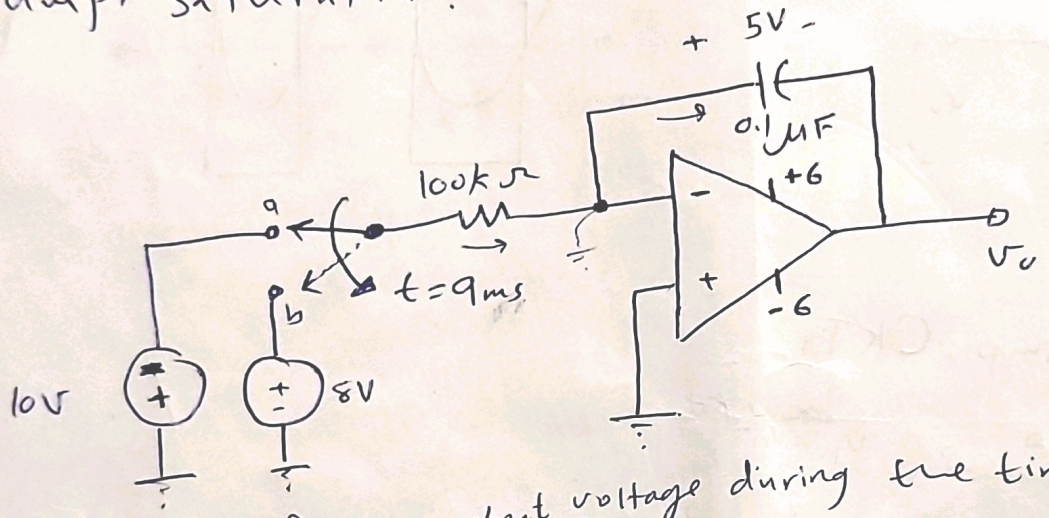
$$V_x = V_{out1} - V_{out2} = 14.29 + 50 = 64.29V$$

ok

10

example

At the instant the switch makes contact with terminal a in the circuit shown in Figure (1), the voltage on the 0.1 μF capacitor is 5 V. The switch remains at terminal a for 9 ms and then moves instantaneously to terminal b. How many ms after making contact with terminal b does the operational amp. saturate.?



The expression for the output voltage during the time the switch is at terminal a is

$$V_o = -\frac{1}{RC} \int_{t_0}^t v_s dt + v_o(t_0)$$

$$= -\frac{1}{(10^5)^2} \int_0^t (10) dt - 5$$

$$= (-5 + 1000t) V$$

at $t = 9 \text{ ms}$

$$V_o = -5 + 9 = 4 V$$

The expression for the output voltage after the switch moves to terminal b is

$$V_o = 4 - \frac{1}{10^5} \int_{9 \times 10^{-3}}^t 8 dt = 4 - 800(t - 9 \times 10^{-3})$$

$$= (11.2 - 800t) V$$

$$\Rightarrow 11.2 - 800t_s = -6$$

$$t_s = 21.5 \text{ ms}$$